

# Hypersonic Turbulent Expansion-Corner Flow with Shock Impingement

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Mean and fluctuating surface pressure data were obtained in a Mach 8, turbulent, cold flow past an expansion corner subjected to shock impingement. The expansion corner of 2.5 or 4.25 deg was located at 0.77 m (30.25 in.) from the leading edge of a sharp-edged flat plate, while an external shock, generated by either a 2- or 4-deg sharp wedge, impinged at the corner, or at one boundary-layer thickness ahead or behind the corner. The mean pressure distribution was strongly influenced by the mutual interaction between the shock and the expansion. For example, the upstream influence decreased when the shock impinged downstream of the corner. Also, the unsteadiness of the interactions was characterized by an intermittent region and a local rms pressure peak near the upstream influence. The peak rms pressure fluctuations increased with a larger overall interaction strength. Shock impingement downstream of the corner resulted in lower fluctuation peaks and also in a shorter region of reduced fluctuation levels. These features may be exploited in inlet design by impinging the cowl shock downstream of an expansion corner instead of at the corner. In addition, a limited pitot pressure survey showed a thinning of the boundary layer downstream of the corner.

## Nomenclature

$M$	= Mach number
$p$	= pressure
$U_\tau$	= friction velocity, $\sqrt{\tau_w/\rho_w}$
$x$	= distance measured from corner along test surface, Fig. 1
$y$	= distance normal to the test surface
$Z$	= standardized pdf variable, $p'/\sigma_p$
$\alpha$	= corner angle, Fig. 1
$\delta$	= boundary-layer thickness
$\theta$	= external wedge angle, Fig. 1
$\sigma_p$	= standard deviation of pressure fluctuations

## Subscripts

$e$	= boundary-layer edge
incip	= incipient
max	= maximum in rms surface pressure distribution
pit	= pitot
pk	= peak
sh	= shock
$u$	= upstream influence
$w$	= mean wall value
0	= undistributed boundary-layer conditions at the corner location
1, 2, 2', 3, 4	= inviscid regions, Fig. 1
$\infty$	= incoming freestream or incoming static value

## Superscripts

'	= fluctuating value
-	= normalized by $\delta_0$

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## Introduction

**S**HOCK wave, boundary-layer interactions have been the subject of considerable research.<sup>1</sup> Recently, renewed interest in supersonic and hypersonic flight vehicles has necessitated a better physical understanding of such interactions than previously achieved. One reason for this necessity is the increased accuracy required in designing these vehicles using computational methods. Unfortunately, complex shock boundary-layer interactions are among a number of flow phenomena that are barely understood at hypersonic Mach numbers.<sup>2</sup> The motivation of the present study is, therefore, to further the understanding of shock boundary-layer interactions through basic experimental research.

Specifically, the present study examines the hypersonic interaction that exists when a shock impinges near an expansion corner as depicted in Fig. 1. This is an idealized, building-block interaction that models the impingement of a cowl shock near an expansion corner in an inlet at off-design conditions. Although the ultimate goal is to support scramjet inlet design pertaining to airbreathing hypersonic vehicles, the present study is of a smaller scope because the shock-expansion interaction has been rarely studied. Hence, the present study

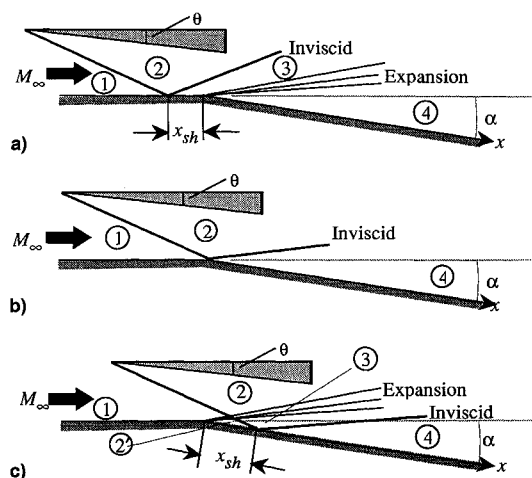


Fig. 1 Schematic of test configurations. Shock reflections a) ahead, b) at, and c) behind expansion corner.

involves small corner and wedge angles giving rise to unseparated interactions. Before discussing the results of the study, brief details of the experiment are outlined next.

## Experiment

### Shock Tunnel

The University of Texas at Arlington (UTA) shock tunnel is of conventional design and consists of a shock tube connected to a nozzle, test section, diffuser, and dump tank as shown in the schematic of Fig. 2. The driver section of the shock tube had a 152-mm (6-in.) bore and was 3 m (10 ft) long. It was connected to the driven section, consisting of three 2.7-m (9-ft) long tubes of 152-mm (6-in.) bore, via a double-diaphragm section. Flow was initiated by rupturing the diaphragms that initially separated the driver and driven gases. The double-diaphragm arrangement provided precise control of the driver and driven pressures, which in turn ensured repeatable stagnation conditions and unit Reynolds number.

A secondary diaphragm of thin Mylar® or aluminum foil was used to separate the driven tube and the nozzle. Once the secondary diaphragm was ruptured, the test gas in the driven tube was expanded by a conical nozzle with a 7.5-deg half-angle expansion to Mach 8 in a semifreejet test section 0.54 m (21 in.) long and 0.44 m (17.5 in.) in diam. The conical nozzle supplied an acceptably uniform flow; Pitot surveys 0.33 m (13 in.) from the leading edge of the flat-plate test model showed that the inviscid core was about 0.17 m (6.7 in.) in diam. Further details of the UTA shock tunnel can be found in Ref. 3.

### Test Model

A stainless steel, flat plate 203 mm (8 in.) wide by 0.96 m (37.75 in.) long, with a sharp convex corner 768 mm (30.25 in.) from its leading edge, was used to develop a boundary layer naturally. The flat plate was mounted 50 mm (2 in.) below the tunnel centerline. Fences under the plate were used to prevent crossflows. In the test region, starting at about 750 mm (29.5 in.) from the flat-plate leading edge, the surface pressure without the corner exhibited an extremely slight, favorable longitudinal pressure gradient as shown in Fig. 3.<sup>4</sup> Within experimental accuracy, the undisturbed surface pressure was assumed uniform.

Two instrumentation plates with  $2.5$  and  $4.25 \pm 0.1$  deg expansion angles were fabricated for surface pressure mea-

surements. Taps for flush-mounted transducers were drilled perpendicularly onto the test surface from 38.1 mm (1.5 in.) upstream to 60.3 mm (2.375 in.) downstream of the corner location. The taps were offset from the centerline by 3.18 mm (0.125 in.) and were spaced 6.35 mm (0.25 in.) or 0.58<sub>0</sub> apart.

An impinging shock was generated by a sharp wedge. This wedge consisted of a sharp-edged plate and an angle-of-attack adapter. The plate was made of aluminum and it was 130 mm (5.25 in.) long and 180 mm (7 in.) wide, which enabled it to span the test region, while its length ensured that expansion waves from the trailing edge impinged on the test surface downstream of the region of interest. The plate was tightened to an adapter to obtain the desired wedge angle of  $2$  or  $4 \pm 0.1$  deg. The wedge assembly was mounted to a sting and the shock impingement position was adjusted to be at the expansion corner, or one boundary-layer thickness upstream and downstream of the corner as shown in Fig. 1. This figure also shows the inviscid wave pattern. Although Figs. 1b and 1c depict a reflected shock, other possibilities, depending on the values of  $\alpha$  and  $\theta$ , include a reflected expansion fan or a shock cancellation. Moreover, for consistency, the inviscid region downstream of the shock boundary-layer interaction is denoted as region 4 in Figs. 1a–1c.

### Data Acquisition and Instrumentation

For dynamic surface pressure measurements, Kulite® model XCS-093-5A and XCS-093-15A pressure transducers were mounted flush to the test surface to better than  $\pm 0.005\delta_0$  to minimize flow interference.<sup>5</sup> Data from the pressure transducers were preconditioned by Leyh model 29 amplifier and anti-aliasing filter combinations with a gain of 500 and a roll-off frequency of 100 kHz before being sent to two LeCroy® model 6810 4-channel, 12-bit waveform recorders. Built-in programmable amplifiers were used to further condition the signals, which were then digitized at 1 Msamples/s/channel and stored within the recorders. The data were subsequently transferred to an Everex® Step 286 host computer that also controlled the data acquisition system. The limited number of channels meant that a detailed pressure distribution was obtained through a number of runs. Seven channels were used to measure interaction surface pressures, whereas the eighth was used to measure a reference pressure  $p_\infty$  34.9 mm (1.375 in. or  $2.6\delta_0$ ) ahead of the corner. The measured interaction pressures were normalized by  $p_\infty$  to minimize the effects of run-to-run variations. Unused orifices were plugged with dummy transducer replicas made from steel rods.

The transducer models used have natural frequencies of 100 and 150 kHz, respectively, as quoted by the manufacturer, whereas the diameter of their sensing surfaces is 0.97 mm (0.038 in.). These characteristics have a bearing on the ability of the transducers to resolve pressure fluctuations. According to Corcos,<sup>6</sup> the maximum measurable frequency for transducers of this size in the present test conditions is about 280 kHz, which cannot be attained due to the lower natural frequencies that these transducers possess. To obtain reliable dynamic data, the data were digitally filtered with a cutoff at 100 kHz before analysis was performed on them. Moreover, the limited spatial resolution of the present transducers resulted in these transducers capturing only 60% of the rms compared to an ideal transducer.<sup>7</sup> Further details on the resolution of surface pressure fluctuations in the present experiments can be found in Ref. 8.

Even though the transducers were used for dynamic measurements, a static calibration sufficed in determining the calibration coefficients.<sup>9</sup> In addition, the signal-to-noise ratio of the transducers was estimated to be about 20 dB (10:1) for  $p < 0.3$  kPa (0.05 psia). However, the magnitude of the pressure signals increased substantially with shock impingement, which consequently improved the signal-to-noise ratio to about 40 dB.<sup>10</sup>

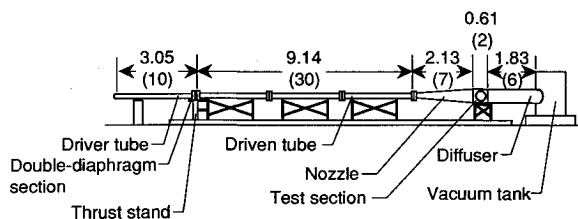


Fig. 2 Schematic of shock tunnel [dimensions in m (ft)].

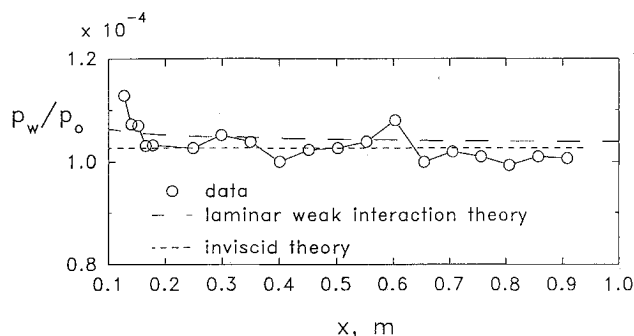


Fig. 3 Flat plate surface pressure distribution.

Pitot pressure surveys were made with a boundary-layer rake. The rake consisted of four pitot probes with Kulite pressure transducers pressed into stainless steel tubes at 18 mm (0.7 in.) from the tip to ensure a fast response. The probes were held in place by small beads of silicone sealant at their rear. A schematic of a pitot probe is shown in Fig. 4a. The inside dimensions of the flattened intake were a width of 1.9 mm (0.075 in.) and a height of 0.25 mm (0.01 in.), with the small height minimizing displacement effects. The pitot probes were installed in one side of a rake housing as shown schematically in Fig. 4b, the other side of the housing being unused. The probes protruded through a slot and faced the incoming flow perpendicularly. The entire rake housing could be moved in small variable steps, accurate to 0.05 mm (0.002 in.) within a pitot rake assembly, and the housing was locked in place by a number of set screws. By stepping the rake, a pitot pressure profile was built up in 4–5 runs. The boundary-layer pitot pressure was normalized by a freestream pitot pressure measured just outside of the boundary layer, and the normalized pitot pressure was accurate to  $\pm 5\%$ .

#### Test Conditions

The tunnel was operated by first charging the driver tube and the double-diaphragm section to 24 MPa  $\pm 1.5\%$  (3500 psia) and 12 MPa (1750 psia), respectively. The driven tube was charged to 280 kPa (40 psia)  $\pm 1.3\%$  after being evacuated to remove moist ambient air. The nozzle, test section, diffuser, and the dump tank were evacuated to less than 0.32 kPa (0.05 psia). The gas used throughout the tunnel was dried air. Such a procedure did not allow the maximum possible run time to be achieved as in the tailored-interface mode of operation,<sup>11</sup> but was implemented to reduce cost and simplify operations. Instead, the useful test time was about 0.5 ms, and it provided the lower cutoff frequency to the test data of about 2 kHz.

Breaking the two diaphragms by venting the double-diaphragm section started the tunnel whereby a shock propagated into the driven tube and an unsteady expansion wave propagated into the driver tube. The shock Mach number  $M_s$  was found to be 2.15 with a run-to-run variation of less than  $\pm 5\%$ ; the low shock Mach number ensured that real gas effects were negligibly small. From the shock Mach number and the initial driver and driven conditions, the stagnation pressure and temperature were estimated as 5.38 MPa (780 psia) and 800 K (1440°R), respectively, to an accuracy of 2–5%, whereas the unit Reynolds number was estimated as  $10.2 \times 10^6 \text{ m}^{-1}$  ( $3.1 \times 10^6/\text{ft}$ ). The flat plate was at room temperature ( $T_w \approx 290 \text{ K}$ , 522°R), and thus, the experiments were performed under cold-wall conditions ( $T_w/T_0 \approx 0.35$ ).

An undisturbed boundary layer developed naturally on the flat plate. From pitot pressure surveys, the boundary-layer thickness at the corner location was determined to be  $12.7 \pm 2 \text{ mm}$  ( $0.50 \pm 0.08 \text{ in.}$ ).<sup>4</sup> Through the test region, the bound-

ary layer possessed a Reynolds number of  $1.8 \times 10^3$  to  $2.3 \times 10^3$ , based on the momentum thickness. This low Reynolds number was manifested by a turbulent boundary layer with a negligible wake.

## Results and Discussion

#### Mean Surface Pressure

Surface pressures are normalized by the incoming free-stream static pressure  $p_\infty$  and are plotted in Figs. 5 and 6, respectively. In each figure, the surface pressure distribution

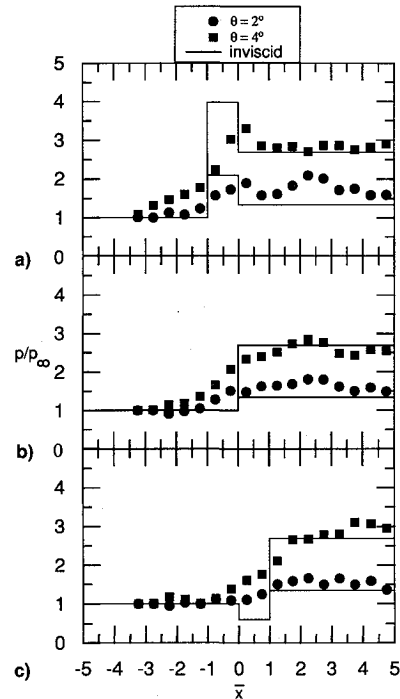


Fig. 5 Shock impingement near 2.5-deg expansion corner.  $\bar{x}_{sh}$  = a) -1, b) 0, and c) 1.

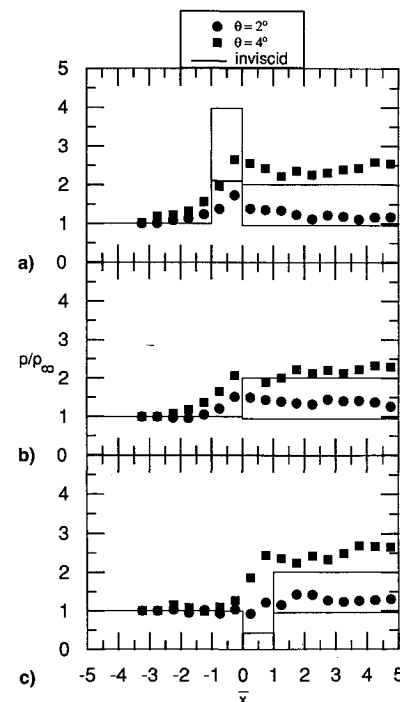


Fig. 6 Shock impingement near 4.25-deg expansion corner.  $\bar{x}_{sh}$  = a) -1, b) 0, and c) 1.

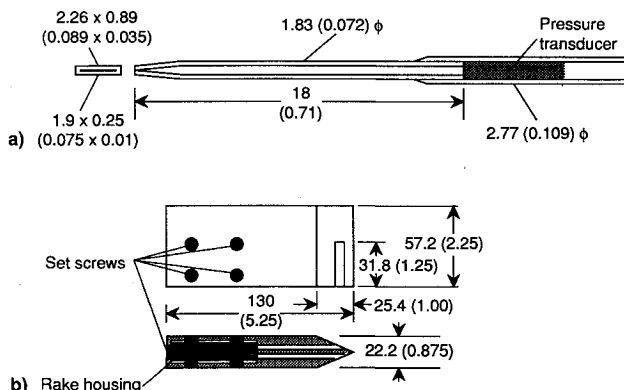


Fig. 4 Schematic of a) pitot probe and b) boundary-layer rake assembly [all dimensions in mm (in.)].

for the three shock impingement locations of  $\bar{x}_{sh} \equiv x_{sh}/\delta_0 = -1, 0$ , and  $1$ , are presented. The inviscid pressure distributions are shown as solid lines.

With the incident shock upstream of the expansion corner, Figs. 5a and 6a show that the surface pressure gradually increases from the upstream influence of the shock, but it does not reach the downstream, inviscid, reflected shock value  $p_3/p_1$ . (The upstream influence is defined as the maximum tangent of the foremost pressure distribution with the incoming pressure level.<sup>12</sup>) Unlike shock reflection off a flat surface, the close proximity of the expansion corner prevents the surface pressure from attaining the downstream inviscid shock value. Moreover, the surface pressure maxima is reduced with a stronger expansion. For  $\theta = 4$  deg,  $p_3/p_1 = 4.05$ , while the peak pressure  $p_{pk}/p_\infty \approx 3.4$  when  $\alpha = 2.5$  deg, and is only  $2.6$  when  $\alpha = 4.25$  deg, representing decreases of  $16$  and  $36\%$ , respectively. For  $\theta = 2$  deg, the peak pressure decreases by  $10$  and  $18\%$  from  $p_3/p_1 = 2.10$  for the two respective corners. This observation indicates that the expansion corner serves to attenuate the interaction pressure rise that would otherwise occur.

Downstream of the expansion corner, the surface pressure tends to the inviscid value. In Ref. 13, a corner "downstream influence"  $\bar{x}_D$  is defined as the intercept between the slope of the downstream pressure distribution and the downstream inviscid value, and it is shown that for flow past an expansion corner, the downstream influence increases with  $\alpha$  or a decrease of the inviscid pressure ratio  $p_4/p_1$ . Although this is difficult to determine in the present experiments due to the gentle pressure gradient,  $\bar{x}_D \approx 1-2$ . This is shorter than that of a pure, expansion corner in which  $\bar{x}_D \approx 5-6$  for the same test conditions.<sup>13</sup> Unlike expansion corner flows where  $p_4/p_1 < 1$ , the decreased downstream influence in the present experiments is thought to be a consequence of the downstream pressure being higher than the incoming value. Moreover, the shock boundary-layer interaction ahead of the corner modifies the boundary layer approaching the corner in such a way as to cause a decrease in the downstream influence. (The detailed physical mechanisms for such a decrease are presently unknown.)

The upstream surface pressure distribution when the shock impinges right at the corner appears similar to that when the shock impinges ahead of the corner, except for a small reduction in upstream influence, compare Figs. 5b and 6b with Figs. 5a and 6a; this will be elaborated later. Under certain conditions in which  $p_4/p_1 \approx 1$ , the pressure distribution due to the reflected shock wave is nearly "neutralized" by the Prandtl-Meyer expansion, as observed previously by Chew.<sup>14</sup>

When the shock impinges downstream of the corner, Figs. 5c and 6c, the surface pressure distribution shows a smaller upstream influence as compared to the other configurations. This decrease in the upstream influence shows that the expansion corner plays an important role in the shock boundary-layer interaction through modifying the incoming boundary-layer characteristics. According to Elfstrom,<sup>15</sup> the upstream propagation of pressure at incipient separation depends on the incoming Mach number and on the Reynolds number based on wall conditions  $Re_w = U_\infty \delta / \nu_w$ . The upstream influence decreases with an increase in  $Re_w$ , and this behavior may be expected to hold for attached interactions as well. For small expansion corners in hypersonic, high Reynolds number flow, the friction velocity and the dynamic viscosity at the wall do not differ greatly from incoming values.<sup>16</sup> However, the expansion produces a thickening of the boundary layer,<sup>10</sup> and thereby, an increase in  $Re_w$ . Consequently, the upstream influence is decreased based on Elfstrom's analysis.

Figures 5c and 6c also show that although the inviscid pressure distribution consists of a pressure drop followed by a pressure rise, the actual pressure distribution for all four cases does not show any significant pressure decrease due to the expansion. (It may be possible that there may be insufficient

data to discern the pressure decrease.) It appears that in a hypersonic expansion flow, the surface pressure decreases in a more uniform fashion due to the highly swept expansion fan. This is unlike Chew's observation<sup>14</sup> in a supersonic flow where the separate effects of the shock and expansion fan can be distinguished clearly when these waves were separated by about  $1.5-2.5\delta_0$ . The separate wave structure due to the expansion and the shock in a hypersonic flow is expected to be achieved only when the shock impinges upon the corner further downstream.

The surface pressure with a  $4.25$ -deg expansion for both impinging shocks shows an overshoot compared with inviscid pressure levels.<sup>14</sup> The pressure distributions arising from the same shocks impinging on a flat plate<sup>10</sup> or the weaker expansion corner, however, do not exhibit the overshoot. This overshoot appears to be a unique feature arising from the mutual interactions of the incident shock and the expansion fan. The suggestion that the overshoot is due to three-dimensional effects arising from tunnel side-wall interactions does not appear feasible in the present unseparated interactions.<sup>14</sup> No explanations, unfortunately, are forthcoming at the moment for this phenomenon.

To quantify the above observations on the upstream influence, the normalized upstream influence  $\bar{x}_u \equiv \bar{x}_u/\delta_0$  is plotted against  $\bar{x}_{sh}$  in Fig. 7. The upstream influence is larger for a higher shock strength as expected. For the same shock strength, when the shock impinges downstream, the upstream influence decreases. The decrease of upstream influence for the weaker incident shock is, however, extremely slight. The expansion corner affects the upstream influence in two ways. First is the proximity of the corner; as the shock impinges from ahead to behind the corner, the upstream influence decreases. Secondly, the stronger the expansion, the smaller the upstream influence.

#### Surface Pressure Fluctuations

The rms distributions of pressure fluctuations are shown in Figs. 8 and 9. The rms distribution of pressure fluctuations  $\sigma_p$  is normalized by the local surface pressure  $p$ . The normalized rms distribution with shock impingement at  $\bar{x}_{sh} = -1$  shows some similar features with one another, e.g., the "peak" rms pressure fluctuation associated with the strong intermittent behavior of the interaction, a damping downstream of the expansion corner, and an increase at  $\bar{x} \approx 3.3-4.2$ . This downstream increase of the surface pressure fluctuations may be due to a change of the boundary-layer state, from one that is "relaminarizing" due to the favorable pressure gradient to one that is "retransitioning" as the boundary layer redevelops to a new equilibrium turbulent state. The downstream peak

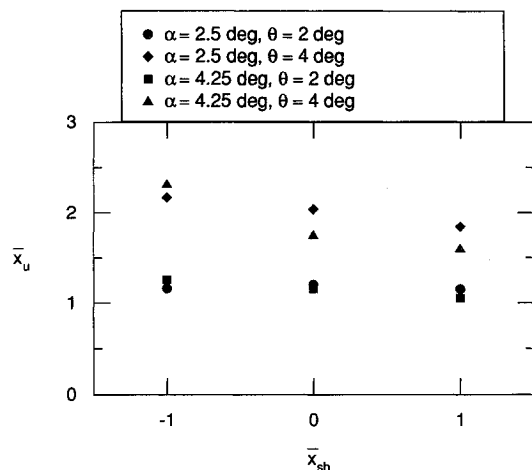


Fig. 7 Upstream influence due to shock impingement near expansion corners.

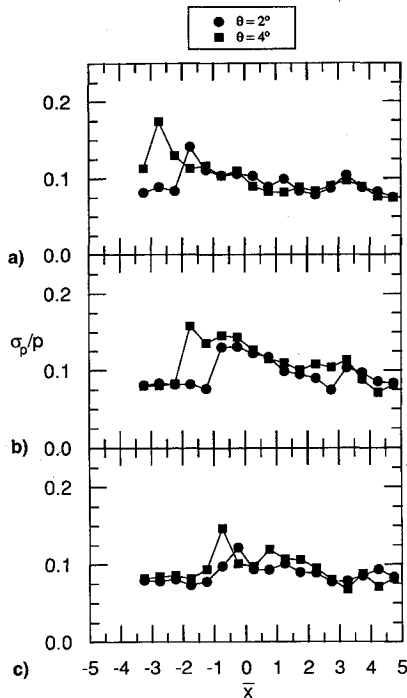


Fig. 8 Root-mean-square pressure distribution due to shock impingement near 2.5-deg expansion corner.  $\bar{x}_{sh}$  = a) -1, b) 0, and c) 1.

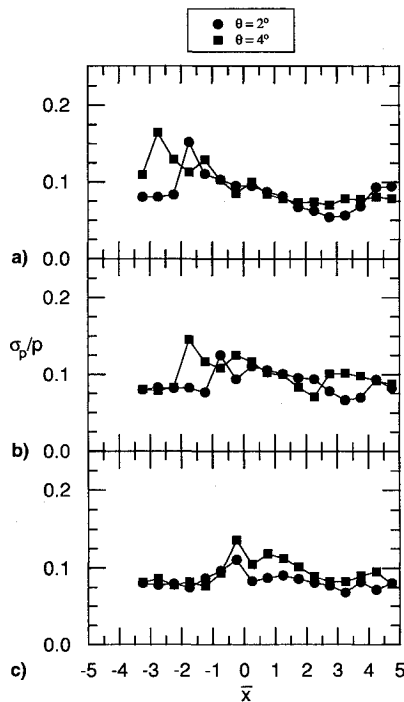


Fig. 9 Root-mean-square pressure distribution due to shock impingement near 4.25-deg expansion corner.  $\bar{x}_{sh}$  = a) -1, b) 0, and c) 1.

in  $\sigma_p$ , also appears related to the downstream peak in mean pressure.

When the shock impinges right at the expansion corner, the characteristic shape of the rms pressure distribution is basically the same as that of shock impingement upstream of the expansion corner. However, the "neutralization" of the shock by the expansion fan reduces the rms peak. For  $\alpha = 4.25$  deg and  $\theta = 2$  deg,  $(\sigma_p/p)_{\max}$  is about 20% below the peak value achieved when the shock impinges upstream of the corner. The rms pressure distribution when the shock impinges downstream of the corner shows the effect of the

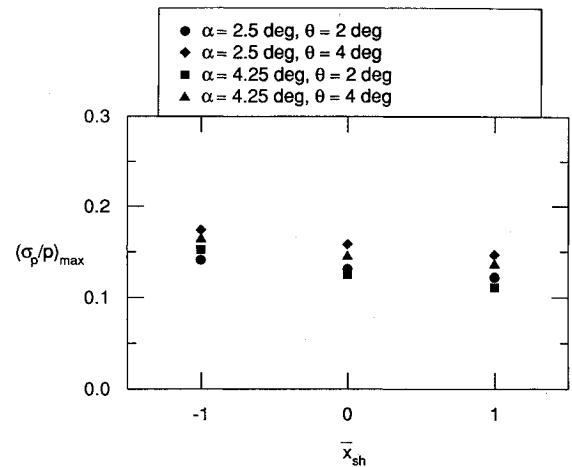


Fig. 10 Peak values of rms pressure.

expansion in attenuating the peak rms value and, further, results in a more severe damping of the fluctuations throughout the downstream region.

The peak rms value  $(\sigma_p/p)_{\max}$  is plotted against  $\bar{x}_{sh}$  in Fig. 10. The figure shows that generally the peak rms value decreases as the impinging shock moves downstream. Although at  $\bar{x}_{sh} = 0$  and 1, the peak rms for the  $\alpha = 4.25$  deg and  $\theta = 2$  deg case is higher than the  $\alpha = 2.5$  deg and  $\theta = 2$  deg case, the data are within experimental error since the actual maximum rms value may not be captured due to the transducer spacing. This decrease in peak rms pressure level, in addition to the lower mean pressure levels, may be exploited in inlet design where the cowl shock is allowed to impinge downstream of an expansion corner under on-design conditions.

The increase in surface pressure fluctuations is thought to be due to shock motion,<sup>17</sup> and can be further understood through examining the probability density functions. Examples of probability distribution functions (pdfs) normalized by the mean local pressure are plotted in Figs. 11 and 12 against  $Z$ . The normalized Gaussian distribution is plotted as a solid line in these figures. The pdfs show a departure from the Gaussian downstream of the interaction onset in which a highly skewed distribution is obtained followed by a bimodal one. These features indicate the presence of an intermittent pressure distribution in which the pressure "switches" from an upstream, lower value, to a downstream, higher value.<sup>17</sup> Also, a comparison of Figs. 11 and 12 reveals that the upstream propagation of disturbances due to the 4-deg wedge is further than that due to the 2-deg wedge. Thus, the pdfs show a larger upstream influence due to the stronger shock interaction as in the mean pressure distribution.

#### Pitot Pressure Surveys

Pitot pressure surveys were performed for only two test conditions, namely, where the oblique shock impinged at the 2.5-deg expansion corner. The inviscid solution provides for a shock reflection in both cases. The pitot pressure, normalized by the value at the boundary-layer edge  $p_{pit,e}$ , is plotted against the perpendicular distance from the wall, normalized by the local boundary-layer thickness, in Fig. 13. The profiles were obtained from  $\bar{x} = 0.75$ – $2.75$  (4.8–35 mm or 0.375–1.375 in.) downstream of the corner. The profiles for both wedge angles show a fairly similar shape. A distortion, whose limits are indicated by a pair of arrowheads in the first profile of Fig. 13a, is observed. This distortion, which is thought to be associated with reflected compression waves, is smeared through the boundary layer and is less distinct compared with those found in pitot surveys of flat plate flow with shock impingement.<sup>10,18</sup> The compression wave system is reflected at a shallow angle and remains embedded within the boundary

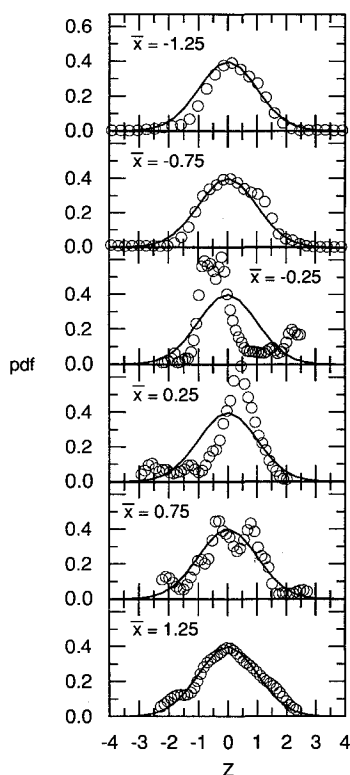


Fig. 11 Probability distribution functions of shock impingement downstream of 2.5-deg expansion ( $\theta = 2$  deg,  $\bar{x}_{sh} = 1$ ).

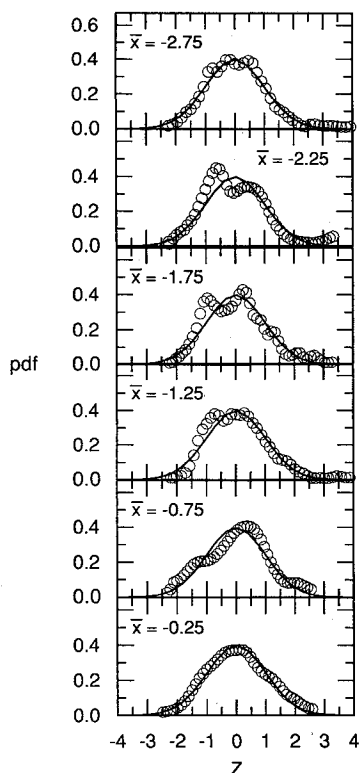


Fig. 12 Probability distribution functions of shock impingement downstream of 2.5-deg expansion ( $\theta = 4$  deg,  $\bar{x}_{sh} = 1$ ).

layer even at  $2.75\delta_0$  from the corner. This is thought to be due to the hypersonic nature of the flow where Mach waves are highly inclined to the incoming flow and which is unlike the steeper wave systems of supersonic flows.<sup>14</sup>

Further, boundary-layer thicknesses extracted from the pitot pressure profiles are shown in Fig. 14. The boundary-layer

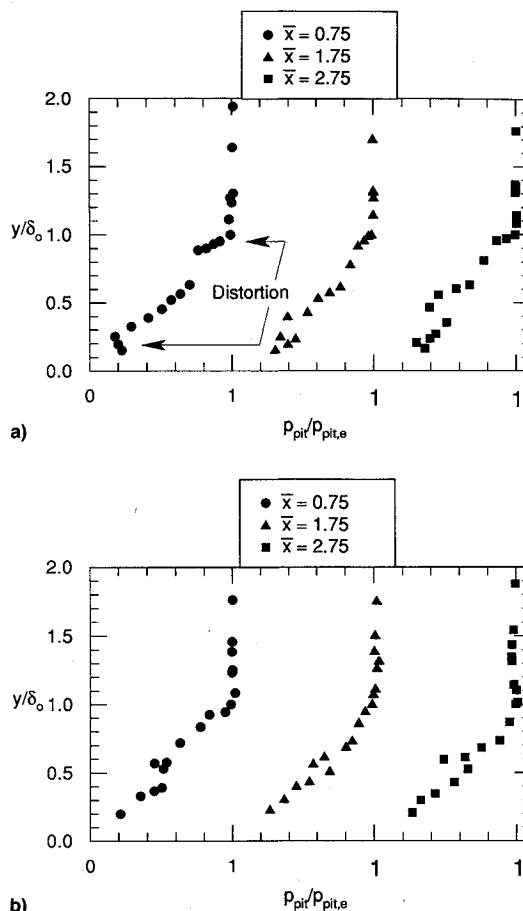


Fig. 13 Pitot pressure profiles for shock impingement on 2.5-deg expansion corner: a)  $\alpha = 2.5$  deg,  $\theta = 2$  deg and b)  $\alpha = 2.5$  deg and  $\theta = 4$  deg.

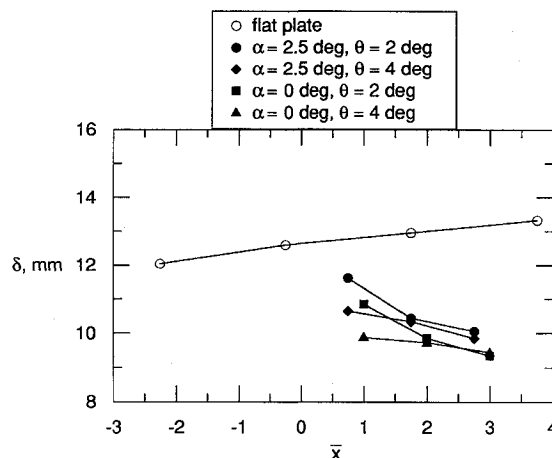


Fig. 14 Boundary-layer thickness due to shock impingement at an expansion corner.

thickness decreases downstream of the corner. For flow past an expansion corner only, the boundary layer thickens more rapidly than that past a flat plate.<sup>10</sup> The more rapid increase is due to a reduction of density through the expansion fan.<sup>19</sup> However, when a shock impinges on the corner, the downstream boundary-layer thickness is reduced. This resembles that of a weak shock impinging on a flat plate.<sup>1</sup>

## Conclusions

A complicated interaction exists when a shock impinges near an expansion corner in a hypersonic flow. This is because the shallow wave systems in a hypersonic flow creates a higher

degree of coupling between the shock-expansion interaction than in a supersonic flow. The favorable pressure gradient set up by the expansion attenuates the upstream influence and limits the surface pressure from reaching the downstream inviscid shock value. The expansion also reduces the unsteadiness inherent in shock, turbulent boundary-layer interactions, including unseparated ones. Moreover, even when the mean surface pressure shows shock cancellation by the expansion fan, a peak still exists in the rms distribution. It appears that the expansion corner has the largest effect on the shock boundary-layer interaction if the shock impinges behind the corner.

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